An introduction to R
Sponsored by
The Association of Psychological Science
and
Society of Multivariate Experimental Psychology

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What is R?

A brief example

Basic statistics and graphics

Psychometric

Outline

- 1 What is R?
 - Where did it come from, why use it?
 - Installing R on your computer and adding packages
 - Basic R capabilities: Calculation, Statistical tables, Graphics
- 2 A brief example
 - A brief example of exploratory and confirmatory data analysis
- Basic statistics and graphics
 - 4 steps: read, explore, test, graph
 - Basic descriptive and inferential statistics
 - \bullet t-test, ANOVA, χ^2
 - Linear Regression
- Psychometrics and beyond
 - Classical Test measures of reliability
 - Multivariate Analysis and Structural Equation Modeling
 - Item Response Theory
- Basic R commands
 - Useful functions



R: Statistics for all us

- What is it?
- Why use it?
- Ommon (mis)perceptions of R
- Examples for psychologists
 - graphical displays
 - basic statistics
 - advanced statistics
 - Although programming is easy in R, that is beyond the scope of today



R: What is it?

- R: An international collaboration
- 2 R: The open source public domain version of S+
- R: Written by statistician (and all of us) for statisticians (and the rest of us)
- R: Not just a statistics system, also an extensible language.
 - This means that as new statistics are developed they tend to appear in R far sooner than elsewhere.
 - R facilitates asking questions that have not already been asked.



Statistical Programs for Psychologists

- General purpose programs
 - R
 - S+
 - SAS
 - SPSS
 - STATA
 - Systat
- Specialized programs
 - Mx
 - EQS
 - AMOS
 - LISREL
 - MPlus
 - Your favorite program



Statistical Programs for Psychologists

- General purpose programs
 - R
 - \$+
 - \$A\$
 - \$P\$\$
 - \$TATA
 - \$y\$tat
- Specialized programs
 - Mx (OpenMx is part of R)
 - EQ\$
 - AMO\$
 - LI\$REL
 - MPIu\$
 - Your favorite program



R: A way of thinking

- "R is the lingua franca of statistical research. Work in all other languages should be discouraged."
- "This is R. There is no if. Only how."
- "Overall, SAS is about 11 years behind R and S-Plus in statistical capabilities (last year it was about 10 years behind) in my estimation."

Taken from the R.-fortunes (selections from the R.-help list serve)



R is open source, how can you trust it?

- Q: "When you use it [R], since it is written by so many authors, how do you know that the results are trustable?"
- A: "The R engine [...] is pretty well uniformly excellent code but you have to take my word for that. Actually, you don't. The whole engine is open source so, if you wish, you can check every line of it. If people were out to push dodgy software, this is not the way they'd go about it."
- Q: Are R packages bug free?
- A: No. But bugs are fixed rapidly when identified.
- Q: How does function x work? May I adapt it for my functions.
- A: Look at the code. Borrow what you need.



What is R?: Technically

- R is an open source implementation of S (S-Plus is a commercial implementation)
- R is available under GNU Copy-left
- The current version of R is 3.0.1
- R is a group project run by a core group of developers (with new releases semiannually)

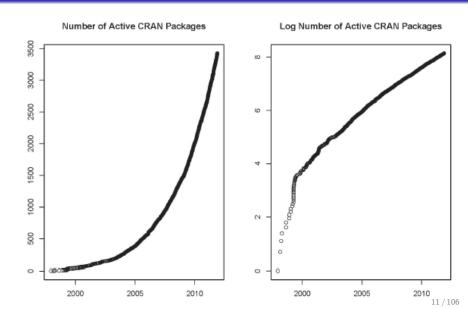
(Adapted from Robert Gentleman)



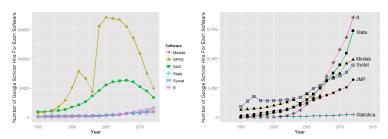
- 1991-93: Ross Dhaka and Robert Gentleman begin work on R project at U. Auckland
- 1995: R available by ftp under the GPL
- 96-97: mailing list and R core group is formed
- 2000: John Chambers, designer of S joins the Rcore (wins a prize for best software from ACM for S)
- 2001-2013: Core team continues to improve base package with a new release every 6 months.
- Many others contribute "packages" to supplement the functionality for particular problems
 - 2003-04-01: 250 packages
 - 2004-10-01: 500 packages
 - 2007-04-12: 1,000 packages
 - 2009-10-04: 2,000 packages
 - 2011-05-12: 3,000 packages
 - 2012-8-27: 4,000 packages
 - 2013-5-12: 4,513 packages (on CRAN)



Rapid and consistent growth in packages contributed to R



Popularity compared to other statistical packages



http://r4stats.com/articles/popularity/ considers various measures of popularity

- discussion groups
- blogs
- Google Scholar citations
- Google Page rank



Misconception: R is hard to use

- R doesn't have a GUI (Graphical User Interface)
 - Partly true, many use syntax.
 - Partly not true, GUIs exist (e.g., R Commander, R-Studio).
 - Quasi GUIs for Mac and PCs make syntax writing easier.
- R syntax is hard to use
 - Not really, unless you think an iPhone is hard to use.
 - Easier to give instructions of 1-4 lines of syntax rather than pictures of what menu to pull down.
 - Keep a copy of your syntax, modify it for the next analysis.
- R is not user friendly: A personological description of R
 - R is introverted: it will tell you what you want to know if you ask, but not if you don't ask.
 - R is conscientious: it wants commands to be correct.
 - R is not agreeable: its error messages are at best cryptic.
 - R is stable: it does not break down under stress.
 - R is open: new ideas about statistics are easily developed.



Misconceptions: R is hard to learn - some interesting facts

- With a brief web based tutorial http://personality-project.org/r, 2nd and 3rd year undergraduates in psychological methods and personality research courses are using R for descriptive and inferential statistics and producing publication quality graphics.
- More and more psychology departments are using it for graduate and undergraduate instruction.
- 3 R is easy to learn, hard to master
 - R-help newsgroup is very supportive
 - Multiple web based and pdf tutorials see (e.g., http://www.r-project.org/)
 - Short courses using R for many applications
- Books and websites for SPSS and SAS users trying to learn R (e.g., http://r4stats.com/) by Bob Muenchen (look for link to free version)).



Ok, how do I get it: Getting started with R

- Download from R Cran (http://cran.r-project.org/)
 - Choose appropriate operating system and download compiled R
- Install R (current version is 3.0.1) (See a tutorial on how to install R and various packages at http://personality-project.org/r/psych)
- Start R
- Add useful packages (just need to do this once)
 - install.packages("ctv") #this downloads the task view package
 - library(ctv) #this activates the ctv package
 - install.views("Psychometrics") #among others
 - Take a 5 minute break
- Activate the package(s) you want to use today (e.g., psych)
 - library(psych) #necessary for most of today's examples
- Use R



What is R? A brief example Basic statistics and graphics Psychometric

Go to the R.project.org



Mhat is R? Contributors Screenshots What's new?

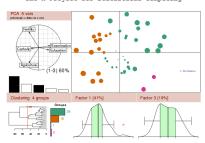
Download, Packages CRAN

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Documentation
Manuals
FAQs
The R Journal
Wiki
Books
Certification
Other

Mise Bioconductor Related Projects User Groups Links

The R Project for Statistical Computing



Getting Started:

- R is a free software environment for statistical computing and graphics. It compiles and runs on a wide variety of UNIX platforms,
- Windows and MacOS. To <u>download R</u>, please choose your preferred <u>CRAN mirror</u>.

 If you have questions about R like how to download and install the software, or what the license terms are, please read our <u>answers to frequently asked questions before you send an email.</u>

News:

- . R 3.0.1 prerelease versions will appear starting May 6. Final release is scheduled for May 16, 2013.
- R version 3.0.0 (Masked Marvel) has been released on 2013-04-03.
 R version 2.15.3 (Security Blanket) has been released on 2013-03-01.
- . The R Journal Vol.4/2 is available.
- useR! 2012, took place at Vanderbilt University, Nashville Tennessee, USA, June 12-15, 2012.
- useR! 2013, will take place at the University of Castilla-La Mancha, Albacete, Spain, July 10-12 2013.





Go to the Comprehensive R Archive Network (CRAN)





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Download and Install R

Precompiled binary distributions of the base system and contributed packages, Windows and Mac users most likely want one of these versions of R:

- Download R for Linux
- Download R for (Mac) OS X
- Download R for Windows
 Download R for Windows

R is part of many Linux distributions, you should check with your Linux package management system in addition to the link above.

Source Code for all Platforms

Windows and Mac users most likely want to download the precompiled binaries listed in the upper box, not the source code. The sources have to be compiled before you can use them. If you do not know what this means, you probably do not want to do list.

- The latest release (2013-05-16, Masked Marvel): R-3.0.1.tar.gz, read what's new in the latest version.
- . Sources of R alpha and beta releases (daily snapshots, created only in time periods before a planned release).
- Daily snapshots of current patched and development versions are <u>available here</u>. Please read about <u>new features and bug</u> fixes before filing corresponding feature requests or bug reports.
- Source code of older versions of R is <u>available here</u>.
- Contributed extension packages

Questions About R

If you have questions about R like how to download and install the software, or what the license terms are, please read
our answers to frequently asked questions before you send an email.

What are R and CRAN?

R is 'GNUS', a freely available language and environment for statistical computing and graphics which provides a wide variety of statistical and graphical techniques: linear and nonlinear modelling, statistical tests, time series analysis, classification, clustering, etc. Please consult the R project homeopage for further information.

CRAN is a network of ftp and web servers around the world that store identical, up-to-date, versions of code and documentation for R. Please use the CRAN of the property to the property of t

Download and install the appropriate version – PC





Subdirectories:

hoso	Binaries for base distribution (managed by Duncan Murdoch). This is what you want to
base	install R for the first time.

CRAN Mirrors What's new?	contrib	Binaries of contributed packages (managed by Uwe Ligges). There is also information on third party software available for CRAN Windows services and corresponding environment and make variables.

Tools to build R and R packages (managed by Duncan Murdoch). This is what you want to Rtools

build your own packages on Windows, or to build R itself.

Please do not submit binaries to CRAN. Package developers might want to contact Duncan Murdoch or Uwe Ligges directly in case of questions / suggestions related to Windows binaries.

You may also want to read the R FAQ and R for Windows FAQ.

Note: CRAN does some checks on these binaries for viruses, but cannot give guarantees. Use the normal precautions with downloaded executables

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Download R 3.0.1 for Windows (52 megabytes, 32/64 bit)

Installation and other instructions New features in this version

If you want to double-check that the package you have downloaded exactly matches the package distributed by R, you can compare the md5sum of the .exe to the true fingerprint. You will need a version of md5sum for windows: both graphical and command line versions are available.

R-3.0.1 for Windows (32/64 bit)

Frequently asked questions

- · How do I install R when using Windows Vista?
- How do I update packages in my previous version of R?
- How do I update packages in my previous version of R?
 Should I run 32-bit or 64-bit R?

Please see the R FAO for general information about R and the R Windows FAO for Windows-specific information.

Other builds

- Patches to this release are incorporated in the r-patched snapshot build.
- A build of the development version (which will eventually become the next major release of R) is available in the <u>r-devel snapshot build</u>.
- Previous releases

Note to webmasters: A stable link which will redirect to the current Windows binary release is <CRAN MIRROR>/bin/windows/base/release.htm.

Last change: 2013-05-16, by Duncan Murdoch

Basic statistics and graphics A brief example Psychometric

Download and install the appropriate version – Mac





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This directory contains binaries for a base distribution and packages to run on Mac OS X (release 10.6 and above), Mac OS 8.6 to 9.2 (and Mac OS X 10.1) are no longer supported but you can find the last supported release of R for these systems (which is R 1.7.1) here. Releases for old Mac OS X systems (through Mac OS X 10.5) and PowerPC Macs can be found in the old directory.

Note: CRAN does not have Mac OS X systems and cannot check these binaries for viruses. Although we take precautions when assembling binaries, please use the normal precautions with downloaded executables.

R 3.0.1 "Good Sport" released on 2013/05/16

This binary distribution of R and the GUI supports 64-bit Intel based Macs on Mac OS X 10.6 (Leopard) or higher,

Since R 3.0.0 the binary is a single-arch build and contains only the x86_64 (64-bit Intel) architecture. PowerPC Macs and 32-bit Macs are only supported by building from sources or by older binary R versions. The default package type is "mag, binary" and the binary repository layout has changed accordingly.

Please check the MD5 checksum of the downloaded image to ensure that it has not been tampered with or corrupted during the mirroring process. For example

nd5 R-3.0.1.pkg in the Terminal application to print the MD5 checksum for the R-3.0.1.pkg image. On Mac OS X 10.7 and later you can also validate the signature using pkgutil --check-signature R-3.0.1.pkg

Files:

R-3.0.1.pkg (latest version) (ca. 65MB)

R 3.0.1 binary for Mac OS X 10.6 (Snow Leopard) and higher, signed package, Contains R 3.0.1 framework, R.app GUI 1.61 in 64-bit for Intel Macs. The above file is an Installer package which can be installed by double-clicking. Depending on your browser, you may need to press the control key and click on this link to download the file.

This package contains the R framework, 64-bit GUI (R.app) and Tcl/Tk 8.6.0 X11 libraries. The latter component is optional and can be ommitted when choosing "custom install", it is only needed if you want to use the toltk R package. GNU Fortran is NOT included (needed if you want to compile packages from sources that contain FORTRAN code) please see the tools directory.

Mac-GUI-1.61.tar.gz

Sources for the R.app GUI 1.61 for Mac OS X. This file is only needed if you want to join the

development of the GUI, it is not intended for regular users. Read the INSTALL file for further instructions.

NEWS (for Mac GUD)

News features and changes in the R.app Mac GUI

The new R.app Cocoa GUI has been written by Simon Urbanek and Stefano Iacus with contributions from many developers and translators world-wide, see "About R" in the GUI

Subdirectories:

universal

Additional tools necessary for building R for Mac OS X:

Universal GNU Fortran compiler for Mac OS X (see R for Mac tools page for details). contrib Binaries of package builds for Mac OS X 10.6 or higher (Snow Leopard build)

Legacy binaries of universal (32-bit and 64-bit) package builds for Mac OS X 10.5 or higher leopard (Leopard build)

Legacy binaries of universal (32-bit) package builds for Mac OS X 10.4 (Tiger build) Previously released R versions for Mac OS X



Starting R on a PC

R Console

R version 2.15.0 (2012-03-30) Copyright (C) 2012 The R Foundation for Statistical Computing TSBN 3-900051-07-0 Platform: i386-pc-mingw32/i386 (32-bit)

R is free software and comes with ABSOLUTELY NO WARRANTY. You are welcome to redistribute it under certain conditions. Type 'license()' or 'licence()' for distribution details.

Natural language support but running in an English locale

R is a collaborative project with many contributors. Type 'contributors()' for more information and 'citation()' on how to cite R or R packages in publications.

Type 'demo()' for some demos, 'help()' for on-line help, or 'help.start()' for an HTML browser interface to help. Type 'q()' to quit R.

>

Start up R and get ready to play (Mac version)

R version 3.0.1 RC (2013-05-12 r62736) -- "Good Sport" Copyright (C) 2013 The R Foundation for Statistical Computing Platform: x86_64-apple-darwin10.8.0 (64-bit)

R is free software and comes with ABSOLUTELY NO WARRANTY. You are welcome to redistribute it under certain conditions. Type 'license()' or 'licence()' for distribution details.

Natural language support but running in an English locale

R is a collaborative project with many contributors.

Type 'contributors()' for more information and
'citation()' on how to cite R or R packages in publications.

Type 'demo()' for some demos, 'help()' for on-line help, or 'help.start()' for an HTML browser interface to help. Type 'q()' to quit R.

[R.app GUI 1.61 (6486) x86_64-apple-darwin10.8.0]

[Workspace restored from /Users/revelle/.RData]
[History restored from /Users/revelle/.Rapp.history]



Annotated installation guide: don't type the >

> install.packages("ctv")

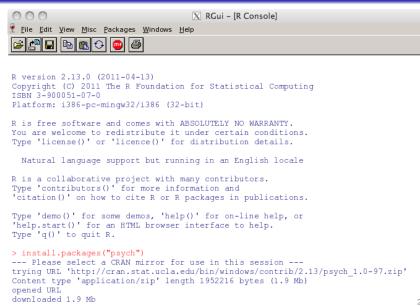
- > library(ctv)
- > install.views("Psychometrics")

#or just install a few packages

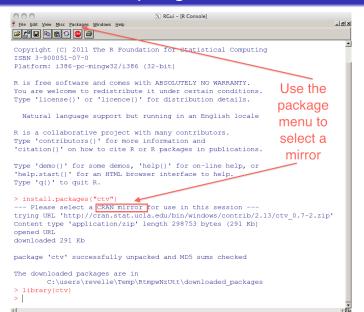
- > install.packages("psych")
- > install.packages("GPArotation")
- > install.packages("MASS")
- > install.packages("mvtnorm")

- Install the task view installer package. You might have to choose a "mirror" site.
- Make it active
- Install all the packages in the "Psychometrics" task view. This will take a few minutes.
- Or, just install one package (e.g., psych)
- as well as a few suggested packages that add functionality for factor rotation, multivariate normal distributions, etc.

Installing just the psych package



Or, install and use ctv package to load a task view on a PC





Check the version number for R (should be \geq 3.0.1) and for psych (\geq 1.3.2)

```
> library(psych)
> sessionInfo()
R version 3.0.1 RC (2013-05-12 r62736)
Platform: x86_64-apple-darwin10.8.0 (64-bit)
locale:
[1] en_US.UTF-8/en_US.UTF-8/en_US.UTF-8/en_US.UTF-8
attached base packages:
[1] stats
             graphics grDevices utils datasets
                                                   methods
                                                             base
other attached packages:
[1] psych_1.3.2
loaded via a namespace (and not attached):
[1] tools 3.0.1
```



R is extensible: The use of "packages"

- More than 4,500 packages are available for R (and growing daily)
- Can search all packages that do a particular operation by using the sos package
 - install.packages("sos") #if you haven't already
 - library(sos) # make it active once you have it
 - findFn("X") #will search a web data base for all packages/functions that have "X"
 - findFn("factor analysis") #will return 9881 matches and reports the top 400
 - findFn("Item Response Theory") # will return 199 matches
 - findFn("INDSCAL") # will return 8 matches.
- install.packages("X") will install a particular package (add it to your R library – you need to do this just once)
- library(X) #will make the package X available to use if it has been installed (and thus in your library)

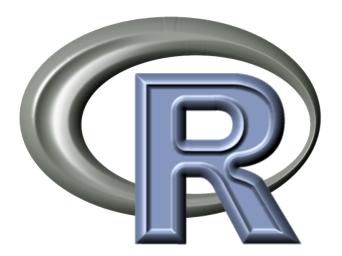


A small subset of very useful packages

- General use
 - core R
 - MASS
 - lattice
 - Ime4 (core)
 - psych
 - Zelig
- Special use
 - Itm
 - sem
 - lavaan
 - OpenMx
 - GPArotation
 - mvtnorm
 - > 3750 known
 - + ?

- General applications
 - most descriptive and inferential stats
 - Modern Applied Statistics with S
 - Lattice or Trellis graphics
 - Linear mixed-effects models
 - Personality and psychometrics
 - General purpose toolkit
- More specialized packages
 - Latent Trait Model (IRT)
 - SEM and CFA (one group)
 - SEM and CFA (multiple groups)
 - SEM and CFA (multiple groups +)
 - Jennrich rotations
 - Multivariate distributions
 - Thousands of more packages on CRAN
 - Code on webpages/journal articles

Questions?





Basic R commands – remember don't enter the >

R is just a fancy calculator. Add, subtract, sum, products, group

- > 2 + 2
- [1] 4
- > 3^4
- [1] 81
- > sum(1:10)
- [1] 55
- > prod(c(1, 2, 3, 5, 7))
- [1] 210

It is also a statistics table (the normal distribution, the t distribution)

- > pnorm(q = 1)
- [1] 0.8413447
- > pt(q = 2, df = 20)
- [1] 0.9703672



R is a set of distributions. Don't buy a stats book with tables!

Table: To obtain the density, prefix with d, probability with p, quantiles with q and to generate random values with r. (e.g., the normal distribution may be chosen by using dnorm, pnorm, qnorm, or rnorm.)

Distribution	base name	P 1	P 2	P 3	example application
Normal	norm	mean	sigma		Most data
Multivariate normal	mvnorm	mean	r	sigma	Most data
Log Normal	Inorm	log mean	log sigma		income or reaction time
Uniform	unif	min	max		rectangular distributions
Binomial	binom	size	prob		Bernuilli trials (e.g. coin flips)
Student's t	t	df		nc	Finding significance of a t-test
Multivariate t	mvt	df	corr	nc	Multivariate applications
Fisher's F	f	df1	df2	nc	Testing for significance of F test
χ^2	chisq	df		nc	Testing for significance of χ^2
Exponential	exp	rate			Exponential decay
Gamma	gamma	shape	rate	scale	distribution theoryh
Hypergeometric	hyper	m	n	k	
Logistic	logis	location	scale		Item Response Theory
Poisson	pois	lambda			Count data
Weibull	weibull	shape	scale		Reaction time distributions



A very small list of the many data sets available

- > data()
- > data(package="psych")

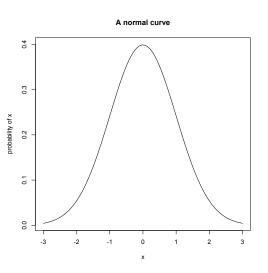
- > data(Titanic)
- > ? Titanic

- > data(cushny)
- > ? cushney

- This opens up a separate text window and lists all of the data sets in the currently loaded packages.
- Show the data sets available in a particular package (e.g., psych).
- Gets the particular data set with its help file (e.g., the survival rates on the Titanic cross classified by age, gender and class).
- 4 Another original data set used by "student" (Gossett) for the t-test.



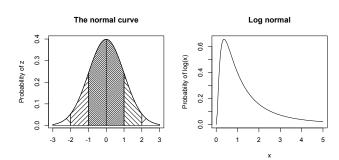
R can draw distributions

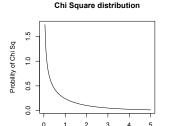


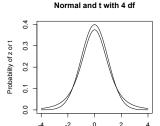
curve(dnormal(x),-3,3, ylab="probability of x",main="A normal curve")



R can draw more interesting distributions









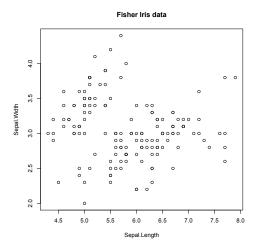
R is also a graphics calculator

The first line draws the normal curve, the second prints the title, the next lines draw the cross hatching.

```
op <- par(mfrow=c(2,2)) #set up a 2 x 2 graph
curve(dnorm(x),-3,3,xlab="",ylab="Probability of z")
title(main="The normal curve",outer=FALSE)
xvals <- seq(-3,-2,length=100)
dvals <- dnorm(xvals)
polygon(c(xvals,rev(xvals)),c(rep(0,100),rev(dvals)),density=2,angle=-45)
xvals <- seq(-2,-1,length=100)
dvals <- dnorm(xvals)
polygon(c(xvals,rev(xvals)),c(rep(0,100),rev(dvals)),density=14,angle=45)
xvals <- seq(-1,-0,length=100)
dvals <- dnorm(xvals)
polygon(c(xvals,rev(xvals)),c(rep(0,100),rev(dvals)),density=34,angle=-45)
xvals <- seq(2,3,length=100)
dvals <- dnorm(xvals)
polygon(c(xvals,rev(xvals)),c(rep(0,100),rev(dvals)),density=2,angle=45)
xvals <- seq(1,2,length=100)
dvals <- dnorm(xvals)
polygon(c(xvals.rev(xvals)).c(rep(0.100).rev(dvals)).density=14.angle=-45)
xvals \leftarrow seq(0.1.length=100)
dvals <- dnorm(xvals)
polygon(c(xvals,rev(xvals)),c(rep(0,100),rev(dvals)),density=34,angle=45)
curve(dlnorm(x),0,5,ylab='Probability of log(x)',main='Log normal')
curve(dchisq(x,1),0,5,ylab='Probility of Chi Sq',xlab='Chi Sq',main='Chi Square distribution')
curve(dnorm(x),-4,4,ylab='Probability of z or t',xlab='z or t',main='Normal and t with 4 df')
curve(dt(x,4),add=TRUE)
op <- par(mfrow=c(1,1))
```



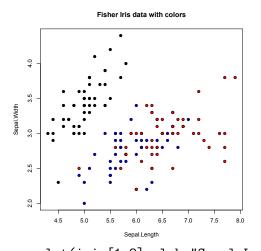
A simple scatter plot using plot



plot(iris[1:2],xlab="Sepal.Length",ylab="Sepal.Width"
,main="Fisher Iris data")



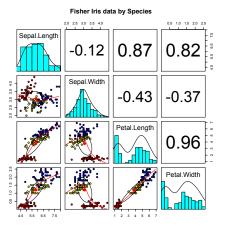
A simple scatter plot using plot with some colors



- Set parameters
- 2 bg for background colors
- open chooses the plot character

plot(iris[1:2],xlab="Sepal.Length",ylab="Sepal.Width"
+ ,main="Fisher Iris data with
colors",bg=c("black","blue","red")[iris[,5]],pch=21)

A scatter plot matrix plot with loess regressions using pairs.panels



- Correlations above the diagonal
- ② Diagonal shows histograms and densities
- scatter plots below the diagonal with correlation ellipse
- locally smoothed (loess) regressions for each pair
- optional color coding of grouping variables.

pairs.panels(iris[1:4],bg=c("red","yellow","blue")
[iris\$Species],pch=21,main="Fisher Iris data by
Species")



A brief example with real data

- Get the data
- ② Descriptive statistics
 - Graphic
 - Numerical
- Inferential statistics using the linear model
 - regressions
- More graphic displays



Get the data and describe it

- First read the data, either from a built in data set, a local file, a remote file, or from the clipboard.
- Describe the data using the describe function from psych

```
> my.data <- sat.act #an example data file that is part of psych
#or
> file.name <- file.choose()</pre>
                                  #look for it on your hard drive
#or
```

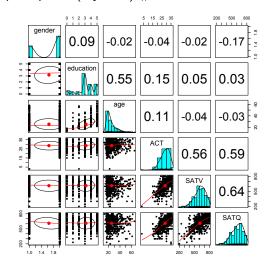
- > file.name <-"http://personality-project.org/r/aps/sat.act.txt" #now read it
- > my.data <- read.table(file.name, header=TRUE)
- #or
- > my.data <- read.clipboard() #if you have copied the data to the clipboard
- > describe(my.data) #report basic descriptive statistics

	var	n	mean	sd	${\tt median}$	${\tt trimmed}$	mad	min	${\tt max}$	range	skew	kurto
gender	1	700	1.65	0.48	2	1.68	0.00	1	2	1	-0.61	-1
education	2	700	3.16	1.43	3	3.31	1.48	0	5	5	-0.68	-0
age	3	700	25.59	9.50	22	23.86	5.93	13	65	52	1.64	2
ACT	4	700	28.55	4.82	29	28.84	4.45	3	36		-0.66	
SATV	5	700	612.23	112.90	620	619.45	118.61	200	800	600	-0.64(-0.59	
SATO	6	687	610.22	115.64	620	617.25	118.61	200	800	600	-0.59	PLO

Psychometric

Graphic display of data using pairs.panels

pairs.panels(my.data) #Note the outlier for ACT





Clean up the data using scrub

- > cleaned <- scrub(my.data,"ACT",min=4)</pre>
- > describe(cleaned)

	var	n	mean	sd	median	trimmed	mad	min	${\tt max}$	range	skew	kurtosis	se
gender	1	700	1.65	0.48	2	1.68	0.00	1	2	1	-0.61	-1.62	0.02
education	2	700	3.16	1.43	3	3.31	1.48	0	5	5	-0.68	-0.06	0.05
age	3	700	25.59	9.50	22	23.86	5.93	13	65	52	1.64	2.47	0.36
ACT	4	699	28.58	4.73	29	28.85	4.45	15	36	21	-0.50	-0.36	0.18
SATV	5	700	612.23	112.90	620	619.45	118.61	200	800	600	-0.64	0.35	4.27
SATO	6	687	610.22	115.64	620	617.25	118.61	200	800	600	-0.59	0.00	4.41



Find the pairwise correlations, round to 2 decimals

- > round(cor(x=sat.act,use="pairwise"),digits=2) #specify a
- > round(cor(cleaned, use="pairwise"),2) #the short way to

	gender	${\tt education}$	age	ACT	SATV	SATQ
gender	1.00	0.09	-0.02	-0.05	-0.02	-0.17
education	0.09	1.00	0.55	0.15	0.05	0.03
age	-0.02	0.55	1.00	0.11	-0.04	-0.03
ACT	-0.05	0.15	0.11	1.00	0.55	0.59
SATV	-0.02	0.05	-0.04	0.55	1.00	0.64
SATQ	-0.17	0.03	-0.03	0.59	0.64	1.00



Display it differently using the lowerCor function

lowerCor finds the pairwise correlations, rounds to 2 decimals, displays the lower half of the correlation matrix, and then abbreviates the column labels to make them line up nicely

> lowerCor(sat.act)

	gendr	edctn	age	ACT	SATV	SATQ
gender	1.00					
${\tt education}$	0.09	1.00				
age	-0.02	0.55	1.00			
ACT	-0.04	0.15	0.11	1.00		
SATV	-0.02	0.05	-0.04	0.56	1.00	
SATQ	-0.17	0.03	-0.03	0.59	0.64	1.00



Test the correlations for significance using corr.test

```
> corr.test(cleaned)
Call:corr.test(x = sat.act)
Correlation matrix
         gender education age
                               ACT SATV SATQ
           1.00
                    0.09 -0.02 -0.04 -0.02 -0.17
gender
education 0.09
                   1.00 0.55 0.15 0.05 0.03
                   0.55 1.00 0.11 -0.04 -0.03
         -0.02
age
ACT
         -0.04
                   0.15 0.11 1.00 0.56 0.59
SATV
         -0.02 0.05 -0.04 0.56 1.00 0.64
SATQ
         -0.17 0.03 -0.03 0.59 0.64 1.00
Sample Size
         gender education age ACT SATV SATQ
gender
           700
                     700 700 700 700 687
                     687 687 687 687 687
SATO
           687
Probability values (Entries above the diagonal are adjusted for multiple tests.
         gender education age ACT SATV SATQ
gender
           0.00
                    0.17 1.00 1.00
education
          0.02
                   0.00 0.00 0.00
age
          0.58
                   0.00 0.00 0.03
ACT
          0.33 0.00 0.00 0.00
                                        0
SATV
          0.62
                   0.22 0.26 0.00
SATO
           0.00
                    0.36 0.37 0.00
                                                                  45 / 106
```

Are education and gender independent? χ^2 Test of association

> chisq.test(T) Pearson's Chi-squared test

- First create a table of associations
 - Do this on our data (my.data)
 - Use the "with" command to specify the data set
- Show the table
- **a** Apply χ^2 test

data:

X-squared = 16.0851, df = 5, p-value = 0.006605



- Use the sat.act data example
- On the linear model
- Summarize the results

```
mod1 <- lm(SATV ~ education + gender + SATQ,data=my.data)</pre>
> summary(mod1,digits=2)
Call:
lm(formula = SATV ~ education + gender + SATQ, data = my.data)
Residuals:
   Min
           1Q Median 3Q
                                 Max
-372.91 -49.08 2.30 53.68 251.93
Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept) 180.87348 23.41019 7.726 3.96e-14 ***
education 1.24043 2.32361 0.534 0.59363
gender 20.69271 6.99651 2.958 0.00321 **
SATO
          0.64489 0.02891 22.309 < 2e-16 ***
Signif. codes: 0 0***0 0.001 0**0 0.01 0*0 0.05 0.0 0.1 0 0 1
Residual standard error: 86.24 on 683 degrees of freedom
  (13 observations deleted due to missingness)
Multiple R-squared: 0.4231, Adjusted R-squared: 0.4205
              167 on 3 and 683 DF, p-value: < 2.2e-16
F-statistic:
```



Zero center the data before examining interactions

In order to examine interactions using multiple regression, we must first "zero center" the data. This may be done using the scale function. By default, scale will standardize the variables. So to keep the original metric, we make the scaling parameter FALSE.

```
zsat <- data.frame(scale(my.data,scale=FALSE))
describe(zsat)</pre>
```

	var	n	${\tt mean}$	sd	median	trimmed	mad	min	max	range	skew
gender	1	700	0	0.48	0.35	0.04	0.00	-0.65	0.35	1	-0.61
education	2	700	0	1.43	-0.16	0.14	1.48	-3.16	1.84	5	-0.68
age	3	700	0	9.50	-3.59	-1.73	5.93	-12.59	39.41	52	1.64
ACT	4	700	0	4.82	0.45	0.30	4.45	-25.55	7.45	33	-0.66
SATV	5	700	0	112.90	7.77	7.22	118.61	-412.23	187.77	600	-0.64
SATQ	6	687	0	115.64	9.78	7.04	118.61	-410.22	189.78	600	-0.59

Note that we need to take the output of scale (which comes back as a matrix) and make it into a dataframe if we want to use the linear model on it.



Zero center the data before examining interactions

```
> zsat <- data.frame(scale(my.data,scale=FALSE))</pre>
> mod2 <- lm(SATV ~ education * gender * SATQ.data=zsat)</pre>
> summary(mod2)
Call:
lm(formula = SATV ~ education * gender * SATQ, data = zsat)
```

Residuals:

```
Min
                                Max
           10
               Median
                          3Q
-372.53 -48.76
                 3.33
                       51.24 238.50
```

Coefficients:

```
Estimate Std. Error t value Pr(>|t|)
(Intercept)
                   0.773576
                            3.304938 0.234 0.81500
education
                   2.517314
                            2.337889 1.077 0.28198
                  18.485906
                            6.964694 2.654 0.00814 **
gender
SATQ
                  education:gender
                 1.249926 4.759374 0.263 0.79292
education:SATQ
                  -0.101444
                            0.020100
                                    -5.047 5.77e-07 ***
gender:SATQ
                  0.007339
                            0.060850
                                     0.121 0.90404
education:gender:SATQ 0.035822
                            0.041192 0.870 0.38481
```



Psychometric

Compare model 1 and model 2

```
Test the difference between the two linear models
```

> anova(mod1,mod2)

Analysis of Variance Table

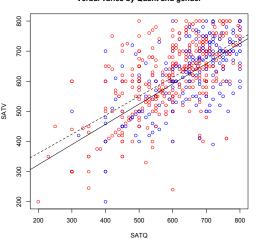
```
Model 1: SATV ~ education + gender + SATQ
Model 2: SATV ~ education * gender * SATQ
 Res.Df
           RSS Df Sum of Sq F Pr(>F)
    683 5079984
2 679 4870243 4 209742 7.3104 9.115e-06 ***
```

Signif. codes: 0 0***0 0.001 0**0 0.01 0*0 0.05 0.0 0.1 0



Show the regression lines by gender

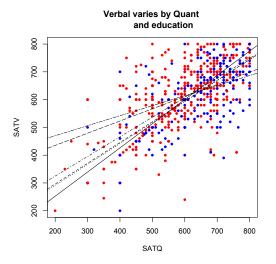
Verbal varies by Quant and gender



- > by(my.data,my.data\$gender, function(x) abline (lm(SATV~SATQ,data=x), lty=c("solid","dashed")

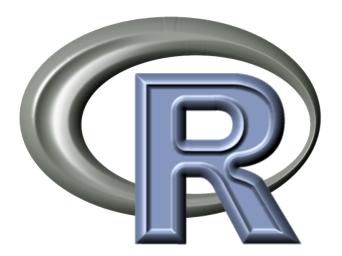


Show the regression lines by education





Questions?





Using R for psychological statistics: Basic statistics

- Writing syntax
 - For a single line, just type it
 - Mistakes can be redone by using the up arrow key
 - For longer code, use a text editor (built into some GUIs)
- ② Data entry
 - Using built in data sets for examples
 - Copying from another program
 - Reading a text or csv file
 - Importing from SPSS or SAS
 - Simulate it (using various simulation routines)
- Oescriptives
 - Graphical displays
 - Descriptive statistics
 - Correlation
- Inferential
 - the t test
 - the F test
 - the linear model



Data entry overview

- Using built in data sets for examples
 - data() will list > 100 data sets in the datasets package as well as all sets in loaded packages.
 - Most packages have associated data sets used as examples
 - psych has > 50 example data sets
- Copying from another program
 - use copy and paste into R using read.clipboard and its variations
- Reading a text or csv file
 - read a local or remote file
- Importing from SPSS or SAS
- Simulate it (using various simulation routines)



Examples of built in data sets from the psych package

> data(package="psych")

Bechtoldt. Seven data sets showing a bifactor solution. Dwyer 8 cognitive variables used by Dwyer for an example. Reise Seven data sets showing a bifactor solution. affect. Data sets of affect and arousal scores as a funct movie conditions (JPSP-12) all.income (income) US family income from US census 2008 bfi 25 Personality items representing 5 factors blot Bond's Logical Operations Test - BLOT 11 emotional variables from Burt (1915) burt. cities Distances between 11 US cities 13 personality scales from the Eysenck Personali epi.bfi and Big 5 inventory income US family income from US census 2008 14 multiple choice IQ items iqitems 75 mood items from the Motivational State Questi msq 3896 participants NEO correlation matrix from the NEO PI R manual neo 3 Measures of ability: SATV, SATQ, ACT sat.act Seven data sets showing a bifactor solution Thurstone Paired comparison of preferences for 9 vegetable veg (vegetables)

Reading data from another program -using the clipboard

- Read the data in your favorite spreadsheet or text editor
- Copy to the clipboard
- Execute the appropriate read.clipboard function with or without various options specified

• read.clipboard() has default values for the most common cases and these do not need to be specified. Consult ?read.clipboard for details.



Reading from a local or remote file

- Perhaps the standard way of reading in data is using the read command.
 - First must specify the location of the file
 - Can either type this in directly or use the file.choose function
 - The file name/location can be a remote URL
- 2 Two examples of reading data

```
file.name <- file.choose() #this opens a window to allow you find the file
my.data <- read.table(file.name)</pre>
```

datafilename="http://personality-project.org/r/datasets/R.appendix1.data" data.ex1=read.table(datafilename, header=TRUE) #read the data into a table

```
> dim(data.ex1) #what are the dimensions of what we read?
[1] 18 2
```

> describe(data.ex1) #do the data look right?

```
sd median trimmed mad min max range skew kurtosi
        1 18 1.89 0.76 2 1.88 1.48 1
                                                    2 0.16
Dosage*
                                             3
```

Alertness 2 18 27.67 6.82 27 27.50 8.15 17 41

24 0.25

read a "foreign" file e.g., an SPSS sav file

read.spss reads a file stored by the SPSS save or export commands.

```
read.spss(file, use.value.labels = TRUE, to.data.frame = FALSE,
    max.value.labels = Inf, trim.factor.names = FALSE,
    trim_values = TRUE, reencode = NA, use.missings = to.data.frame)
```

file Character string: the name of the file or URL to read.

use.value.labels Convert variables with value labels into R factors with those levels?

to.data.frame return a data frame? Defaults to FALSE, probably should be TRUE in most cases

max.value.labels Only variables with value labels and at most this many unique values will be converted to factors if use.value.labels = TRUE.

trim.factor.names Logical: trim trailing spaces from factor levels?

trim_values logical: should values and value labels have trailing spaces ignored

when matching for use.value.labels = TRUE?

use.missings logical: should information on user-defined missing values be used to set the corresponding values to NA?



An example of reading from an SPSS file

- > library(foreign)
- > datafilename <- "http://personality-project.org/r/datasets/finkel.sav"

> describe(eli.skew=FALSE)

	var	n	mean	sd	median	trimmed	mad	\min	${\tt max}$	range	se	
USER*	1	69	35.00	20.06	35	35.00	25.20	1	69	68	2.42	
HAPPY	2	69	5.71	1.04	6	5.82	0.00	2	7	5	0.13	
SOULMATE	3	69	5.09	1.80	5	5.32	1.48	1	7	6	0.22	
ENJOYDEX	4	68	6.47	1.01	7	6.70	0.00	2	7	5	0.12	
UPSET	5	69	0.41	0.49	0	0.39	0.00	0	1	1	0.06	

- Make the foreign package active
- Specify the name (and location) of the file to read
- Read from a SPSS file
- Describe it to make sure it is right



Simulate data

For many demonstration purposes, it is convenient to generate simulated data with a certain defined structure. The *psych* package has a number of built in simulation functions. Here are a few of them.

- Simulate various item structures sim.congeneric A one factor congeneric measure model sim.items A two factor structure with either simple structure or a circumplex structure. sim.rasch Generate items for a one parameter IRT model. sim.irt Generate items for a one-four parameter IRT Model
- Simulate various factor structures sim.simplex Default is a four factor structure with a three time point simplex structure.
 - sim.hierarchical Default is 9 variables with three correlated factors.



Get the data and look at it

Read in some data, look at the first and last few cases (using headtail), and then get basic descriptive statistics. For this example, we will use a built in data set.

```
> mv.data <- epi.bfi
> headtail(my.data)
    epiE epiS epiImp epilie epiNeur bfagree bfcon bfext bfneur bfopen bdi traitanx stateanx
      18
           10
                                           138
                                                        141
                                                                 51
                                                                        138
                                                                                       24
                                                                                                 22
                                   12
                                                                       132
      16
                                           101
                                                        107
                                                                116
                                                                                       41
                                                                                                40
                                           143
                                                  118
                                                                        90
      12
                                                  106
                                                                       101
                                           104
                                                                114
228
      12
                                                  129
                                                        127
                                  15
                                           155
                                                                 88
                                                                       110
                                                                                      35
                                                                                                34
229
      19
           10
                                           162
                                                  152
                                                        163
                                                               104
                                                                                       29
                                                                                                47
                                                                       164
230
                                   10
                                            95
                                                  111
                                                         75
                                                                123
                                                                       138
                                                                                       39
                                                                                                58
231
                                   15
                                            85
                                                   62
                                                                131
                                                                        96
                                                                                       58
                                                                                                58
```

epi.bfi has 231 cases from two personality measures.



Now find the descriptive statistics for this data set

> describe(my.data)

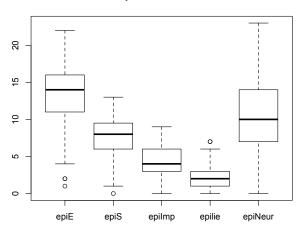
	var	n	mean	sd	median	trimmed	mad	min	max	range	skew	kurtosis	se
epiE	1	231	13.33	4.14	14	13.49	4.45	1	22	21	-0.33	-0.01	0.27
epiS	2	231	7.58	2.69	8	7.77	2.97	0	13	13	-0.57	0.04	0.18
epiImp	3	231	4.37	1.88	4	4.36	1.48	0	9	9	0.06	-0.59	0.12
epilie	4	231	2.38	1.50	2	2.27	1.48	0	7	7	0.66	0.30	0.10
epiNeur	5	231	10.41	4.90	10	10.39	4.45	0	23	23	0.06	-0.46	0.32
bfagree	6	231	125.00	18.14	126	125.26	17.79	74	167	93	-0.21	-0.22	1.19
bfcon	7	231	113.25	21.88	114	113.42	22.24	53	178	125	-0.02	0.29	1.44
bfext	8	231	102.18	26.45	104	102.99	22.24	8	168	160	-0.41	0.58	1.74
bfneur	9	231	87.97	23.34	90	87.70	23.72	34	152	118	0.07	-0.51	1.54
bfopen	10	231	123.43	20.51	125	123.78	20.76	73	173	100	-0.16	-0.11	1.35
bdi	11	231	6.78	5.78	6	5.97	4.45	0	27	27	1.29	1.60	0.38
traitanx	12	231	39.01	9.52	38	38.36	8.90	22	71	49	0.67	0.54	0.63
ctateany	13	231	39 85	11 48	38	38 92	10 38	21	79	58	0.72	0 04	0.76



Boxplots are a convenient descriptive device

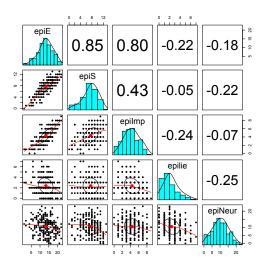
Show the Tukey "boxplot" for the Eysenck Personality Inventory

Boxplots of EPI scales





Plot the scatter plot matrix (SPLOM) of the first 5 variables using the pairs.panels function

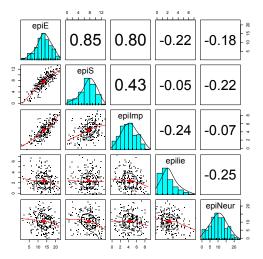


Use the pairs.panels function from psych

pairs.panels(my.data[1:5])



Plot the scatter plot matrix (SPLOM) of the first 5 variables using the pairs.panels function but with smaller pch and jittering the points.



Use the pairs.panels function from *psych*



Find the correlations for this data set, round off to 2 decimal places

```
> round(cor(mv.data, use = "pairwise"), 2)
```

```
epiS epiImp epilie epiNeur bfagree bfcon bfext bfneur bfopen
                                                                               bdi traitanx stateanx
epiE
          1.00
                0.85
                       0.80
                             -0.22
                                     -0.18
                                              0.18 -0.11 0.54
                                                                -0.09
                                                                         0.14 -0.16
                                                                                       -0.23
                                                                                                -0.13
epiS
          0.85
                1.00
                       0.43
                             -0.05
                                     -0.22
                                              0.20 0.05 0.58
                                                                -0.07
                                                                         0.15 -0.13
                                                                                       -0.26
                                                                                                -0.12
                                              0.08 -0.24 0.35
epiImp
          0.80
                0.43
                       1.00
                             -0.24
                                     -0.07
                                                                -0.09
                                                                         0.07 -0.11
                                                                                       -0.12
                                                                                                -0.09
epilie
         -0.22 -0.05
                      -0.24
                              1.00
                                     -0.25
                                              0.17
                                                    0.23 -0.04
                                                                -0.22
                                                                       -0.03 -0.20
                                                                                       -0.23
                                                                                                -0.15
         -0.18 -0.22
                      -0.07
                             -0.25
                                     1.00
                                             -0.08 -0.13 -0.17
                                                                 0.63
                                                                        0.09 0.58
                                                                                       0.73
                                                                                                0.49
epiNeur
bfagree
         0.18 0.20
                       0.08
                              0.17
                                     -0.08
                                              1.00
                                                    0.45 0.48
                                                                -0.04
                                                                         0.39 - 0.14
                                                                                       -0.31
                                                                                                -0.19
bfcon
         -0.11
               0.05
                      -0.24
                              0.23
                                     -0.13
                                              0.45
                                                   1.00 0.27
                                                                 0.04
                                                                         0.31 -0.18
                                                                                       -0.29
                                                                                                -0.14
bfext
         0.54 0.58
                       0.35
                             -0.04
                                     -0.17
                                              0.48
                                                    0.27
                                                          1.00
                                                                 0.04
                                                                        0.46 -0.14
                                                                                       -0.39
                                                                                                -0.15
                                                    0.04
                                                                                                 0.49
bfneur
         -0.09 -0.07
                      -0.09
                             -0.22
                                      0.63
                                             -0.04
                                                          0.04
                                                                 1.00
                                                                         0.29 0.47
                                                                                        0.59
bfopen
         0.14 0.15
                       0.07
                             -0.03
                                      0.09
                                              0.39 0.31 0.46
                                                                 0.29
                                                                         1.00 -0.08
                                                                                       -0.11
                                                                                                -0.04
         -0.16 -0.13
                             -0.20
                                      0.58
                                             -0.14 -0.18 -0.14
                                                                 0.47
                                                                        -0.08 1.00
                                                                                        0.65
                                                                                                 0.61
bdi
                      -0.11
traitanx -0.23 -0.26
                                      0.73
                                                                                        1.00
                                                                                                 0.57
                      -0.12
                             -0.23
                                             -0.31 -0.29 -0.39
                                                                 0.59
                                                                        -0.11 0.65
stateanx -0.13 -0.12
                      -0.09
                             -0.15
                                      0.49
                                             -0.19 -0.14 -0.15
                                                                 0.49
                                                                       -0.04 0.61
                                                                                        0.57
                                                                                                 1.00
```



Find the correlations for this data set, round off to 2 decimal places using lowerCor

> lowerCor(my.data)

```
epiE epiS epImp epili epiNr bfagr bfcon bfext bfner bfopn bdi trtnx sttnx
         1.00
epiE
epiS
         0.85
              1.00
         0.80 0.43 1.00
epiImp
epilie
        -0.22 -0.05 -0.24 1.00
epiNeur -0.18 -0.22 -0.07 -0.25 1.00
bfagree
        0.18 0.20 0.08 0.17 -0.08 1.00
bfcon
        -0.11 0.05 -0.24 0.23 -0.13 0.45 1.00
bfext.
         0.54 0.58 0.35 -0.04 -0.17 0.48 0.27
bfneur
        -0.09 -0.07 -0.09 -0.22 0.63 -0.04 0.04
                                                0.04
        0.14 0.15 0.07 -0.03 0.09 0.39 0.31
bfopen
                                                0.46 0.29 1.00
        -0.16 -0.13 -0.11 -0.20 0.58 -0.14 -0.18 -0.14 0.47 -0.08 1.00
bdi
traitanx -0.23 -0.26 -0.12 -0.23 0.73 -0.31 -0.29 -0.39 0.59 -0.11 0.65 1.00
stateanx -0.13 -0.12 -0.09 -0.15 0.49 -0.19 -0.14 -0.15 0.49 -0.04 0.61 0.57 1.00
```



Test the significance and use Holm correction for multiple tests

```
> corr.test(my.data)
Call:corr.test(x = mv.data)
Correlation matrix
         epiE epiS epiImp epilie epiNeur bfagree bfcon bfext bfneur bfopen bdi traitanx stateanx
epiE
               0.85
                      0.80 -0.22
                                    -0.18
                                             0.18 -0.11 0.54 -0.09
                                                                       0.14 - 0.16
                                                                                     -0.23
                                                                                              -0.13
                                    -0.22
                                                                                     -0.26
                                                                                              -0.12
epiS
         0.85
              1.00
                      0.43 -0.05
                                             0.20 0.05 0.58
                                                               -0.07
                                                                       0.15 -0.13
         0.80 0.43
                      1.00 -0.24
                                    -0.07
                                             0.08 -0.24 0.35
                                                               -0.09
                                                                       0.07 -0.11
                                                                                     -0.12
                                                                                              -0.09
epiImp
stateanx -0.13 -0.12 -0.09 -0.15
                                     0.49
                                            -0.19 -0.14 -0.15
                                                                0.49 -0.04 0.61
                                                                                      0.57
                                                                                               1.00
Sample Size
         epiE epiS epiImp epilie epiNeur bfagree bfcon bfext bfneur bfopen bdi traitanx stateanx
epiE
         231 231
                     231
                             231
                                    231
                                            231
                                                  231
                                                        231
                                                               231
                                                                      231 231
                                                                                   231
                                                                                            231
stateanx 231 231
                     231
                             231
                                    231
                                            231
                                                  231
                                                        231
                                                               231
                                                                      231 231
                                                                                   231
                                                                                            231
Probability values (Entries above the diagonal are adjusted for multiple tests.)
         epiE epiS epiImp epilie epiNeur bfagree bfcon bfext bfneur bfopen bdi traitanx stateanx
epiE
        0.00 0.00
                    0.00
                           0.03
                                   0.27
                                           0.27 1.00 0.00
                                                              1.00
                                                                     1.00 0.59
                                                                                   0.02
                                                                                            1.00
epiS
        0.00 0.00
                    0.00
                           1.00
                                   0.04
                                           0.08 1.00 0.00
                                                              1.00
                                                                     0.62 1.00
                                                                                   0.00
                                                                                            1.00
epiImp 0.00 0.00
                    0.00
                           0.01
                                   1.00
                                           1.00 0.01 0.00
                                                              1.00
                                                                     1.00 1.00
                                                                                   1.00
                                                                                            1.00
epilie
        0.00 0.43
                    0.00
                           0.00
                                   0.01
                                           0.32
                                                0.03 1.00
                                                              0.03
                                                                     1.00 0.08
                                                                                   0.02
                                                                                            0.61
                                                              0.00
epiNeur 0.01 0.00
                    0.26
                           0.00
                                   0.00
                                           1.00 1.00 0.33
                                                                     1.00 0.00
                                                                                   0.00
                                                                                            0.00
bfagree 0.01 0.00
                    0.23
                           0.01
                                   0.21
                                           0.00 0.00 0.00
                                                              1.00
                                                                     0.00 0.95
                                                                                   0.00
                                                                                            0.12
bfcon
        0.08 0.48
                    0.00
                           0.00
                                   0.04
                                           0.00
                                                0.00
                                                      0.00
                                                              1.00
                                                                     0.00 0.25
                                                                                   0.00
                                                                                            1.00
bfext
        0.00 0.00
                    0.00
                           0.50
                                   0.01
                                           0.00 0.00
                                                       0.00
                                                              1.00
                                                                     0.00 0.99
                                                                                   0.00
                                                                                            0.76
bfneur 0.15 0.30
                    0.18
                           0.00
                                   0.00
                                           0.50 0.50 0.57
                                                              0.00
                                                                     0.00 0.00
                                                                                   0.00
                                                                                            0.00
        0.04 0.02
                    0.30
                           0.70
                                   0.19
                                           0.00 0.00 0.00
                                                              0.00
                                                                     0.00 1.00
                                                                                   1.00
                                                                                            1.00
bfopen
bdi
         0.02 0.04
                    0.11
                           0.00
                                   0.00
                                           0.03 0.01
                                                       0.03
                                                              0.00
                                                                     0.25 0.00
                                                                                   0.00
                                                                                            0.00
traitanx 0.00 0.00
                    0.07
                           0.00
                                   0.00
                                           0.00 0.00
                                                       0.00
                                                              0.00
                                                                     0.11 0.00
                                                                                   0.00
                                                                                            0.00(
stateanx 0.05 0.07
                    0.18
                           0.02
                                   0.00
                                           0.00 0.04 0.02
                                                              0.00
                                                                     0.52 0.00
                                                                                   0.00
                                                                                            0.00
```

t.test demonstration with Student's data (from the sleep dataset)

```
> with(sleep,t.test(extra~group))
                   Welch Two Sample t-test
sleep
                   data: extra by group
                   t = -1.8608, df = 17.776, p-value = 0.07939
> sleep
                   alternative hypothesis: true difference in means is not equal
   extra group ID
                  95 percent confidence interval:
     0.7
                2 -3.3654832 0.2054832
2
  -1.6
                3 sample estimates:
3
   -0.2
                   mean in group 1 mean in group 2
4
   -1.2
                              0.75
                                              2.33
5
  -0.1
             1
6
    3.4
                   But the data were actually paired. Do it for a paired t-test
7
     3.7
                   > with(sleep,t.test(extra~group,paired=TRUE))
. . .
13
     1.1
                  Paired t-test
14
     0.1
                  data: extra by group
15 -0.1
                  t = -4.0621, df = 9, p-value = 0.002833
16 4.4
                  alternative hypothesis: true difference in means is not equal
17
    5.5
                  95 percent confidence interval:
18 1.6
               8
                  -2.4598858 -0.7001142
19
    4.6
                   sample estimates:
20
     3.4
             2 10
```

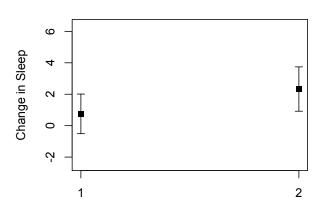
-1.58

70 / 106

mean of the differences

Two ways of showing Student's t test data

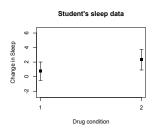
Student's sleep data



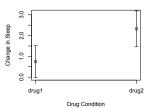


What is R? A brief example Basic statistics and graphics Psychometric

Two ways of showing Student's t test data



Student's paired sleep data



Use the error.bars.by and error.bars functions. Note that we need to change the data structure a little bit to get the within subject error bars.

```
> error.bars.by(sleep$extra,sleep$group,
    by.var=TRUE, lines=FALSE,
    ylab="Change in Sleep", xlab="Drug
    condition",main="Student's sleep data")
```



Analysis of Variance

- aov is designed for balanced designs, and the results can be hard to interpret without balance: beware that missing values in the response(s) will likely lose the balance.
- If there are two or more error strata, the methods used are statistically inefficient without balance, and it may be better to use lme in package nlme.

datafilename="http://personality-project.org/R/datasets/R.appendix2.data" data.ex2=read.table(datafilename,header=T) #read the data into a table data.ex2 #show the data

#show the data

data.ex2					
data.ex2	2				
Observ	ation	${\tt Gender}$	Dosage	Alertness	
1	1	m	a	8	
2	2	m	a	12	
3	3	m	a	13	
4	4	m	a	12	
14	14	f	b	12	
15	15	f	b	18	
16	16	f	b	22	



Analysis of Variance

1 Do the analysis of variances and the show the table of results.

```
aov.ex2 = aov(Alertness~Gender*Dosage,data=data.ex2) #do the analysis of varian
summary(aov.ex2) #show the summary table
```

```
> aov.ex2 = aov(Alertness~Gender*Dosage,data=data.ex2) #do the analysis of va
> summary(aov.ex2) #show the summary table
```

```
Df Sum Sq Mean Sq F value Pr(>F)
Gender 1 76.562 76.562 2.9518 0.1115
Dosage 1 5.062 5.062 0.1952 0.6665
Gender:Dosage 1 0.063 0.063 0.0024 0.9617
```



Show the results table

Gender a

f 15.75 16.75 m 11.25 12.50

```
> print(model.tables(aov.ex2, "means"), digits=3)
Residuals
              12 311.250 25.938
Tables of means
Grand mean
14.0625
Gender
Gender
    f
16.25 11.88
Dosage
Dosage
13.50 14.62
Gender:Dosage
      Dosage
```



Analysis of Variance: Within subjects

- Somewhat more complicated because we need to convert "wide" data.frames to "long" or "narrow" data.frame.
- This can be done by using the stack function. Some data sets are already in the long format.
- A detailed discussion of how to work with repeated measures designs is at

```
http://personality-project.org/r/r.anova.html and
at http://personality-project.org/r
```

See also the tutorial by Jason French at http://gradstudents.wcas.northwestern.edu/ ~jaf502/tutorials/repeatedmeasures.html



Analysis of variance within subjects

```
> datafilename="http://personality-project.org/r/datasets/R.appendix5.data"
> data.ex5=read.table(datafilename, header=T) #read the data into a table
> #data.ex5
                                               #show the data
> aov.ex5 =
+ aov(Recall~(Task*Valence*Gender*Dosage)+Error(Subject/(Task*Valence))+
+ (Gender*Dosage), data.ex5)
> summary(aov.ex5)
Error: Subject
             Df
                 Sum Sq Mean Sq F value Pr(>F)
Gender
                 542.26 542.26 5.6853 0.03449 *
              2 694.91 347.45 3.6429 0.05803 .
Dosage
Gender: Dosage 2 70.80 35.40 0.3711 0.69760
Residuals
             12 1144.56 95.38
Signif. codes: 0 0***0 0.001 0**0 0.01 0*0 0.05 0.0 0.1 0 0 1
Error: Subject:Task
                  Df Sum Sq Mean Sq F value
                                               Pr(>F)
Task
                   1 96.333 96.333 39.8621 3.868e-05 ***
Task:Gender
                   1 1.333 1.333 0.5517
                                              0.4719
Task:Dosage
                   2 8.167 4.083 1.6897
                                              0.2257
```

3.167 1.583 0.6552

12 29.000 2.417

0.5370



Residuals

Task:Gender:Dosage

Multiple regression

- ① Use the sat.act data set from psych
- O the linear model
- Summarize the results

```
mod1 <- lm(SATV ~ education + gender + SATQ,data=sat.act)</pre>
> summary(mod1,digits=2)
Call:
lm(formula = SATV ~ education + gender + SATQ, data = sat.act)
Residuals:
   Min
           1Q Median 3Q
                                 Max
-372.91 -49.08 2.30 53.68 251.93
Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept) 180.87348 23.41019 7.726 3.96e-14 ***
education 1.24043 2.32361 0.534 0.59363
gender 20.69271 6.99651 2.958 0.00321 **
SATO
          0.64489 0.02891 22.309 < 2e-16 ***
Signif. codes: 0 0***0 0.001 0**0 0.01 0*0 0.05 0.0 0.1 0 0 1
Residual standard error: 86.24 on 683 degrees of freedom
  (13 observations deleted due to missingness)
Multiple R-squared: 0.4231, Adjusted R-squared: 0.4205
              167 on 3 and 683 DF, p-value: < 2.2e-16
F-statistic:
```



Zero center the data before examining interactions

```
> zsat <- data.frame(scale(sat.act,scale=FALSE))
> mod2 <- lm(SATV ~ education * gender * SATQ,data=zsat)
> summary(mod2)
Call:
lm(formula = SATV ~ education * gender * SATQ, data = zsat)
```

Residuals:

```
Min 1Q Median 3Q Max -372.53 -48.76 3.33 51.24 238.50
```

Coefficients:

```
Estimate Std. Error t value Pr(>|t|)
(Intercept)
                   0.773576
                            3.304938 0.234 0.81500
education
                   2.517314
                            2.337889 1.077 0.28198
                  18.485906
                            6.964694 2.654 0.00814 **
gender
SATQ
                   education:gender
                 1.249926 4.759374 0.263 0.79292
education:SATQ
                  -0.101444
                            0.020100
                                     -5.047 5.77e-07 ***
gender:SATQ
                  0.007339
                            0.060850 0.121 0.90404
education:gender:SATQ 0.035822
                            0.041192 0.870 0.38481
Signif. codes: 0 0***0 0.001 0**0 0.01 0*0 0.05 0.0 0.1 0 0 1
```



What is R?

```
> anova(mod1,mod2)
```

Analysis of Variance Table

```
Model 1: SATV ~ education + gender + SATQ

Model 2: SATV ~ education * gender * SATQ

Res.Df RSS Df Sum of Sq F Pr(>F)

1 683 5079984

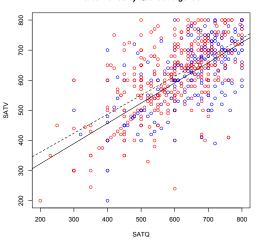
2 679 4870243 4 209742 7.3104 9.115e-06 ***
```

Signif. codes: 0 $\hat{0}***\tilde{0}$ 0.001 $\hat{0}**\tilde{0}$ 0.01 $\hat{0}*\tilde{0}$ 0.05 $\hat{0}.\tilde{0}$ 0.1 $\hat{0}$



Show the regression lines by gender

Verbal varies by Quant and gender



- > by(sat.act,sat.act\$gender, function(x) abline (lm(SATV~SATQ,data=x), lty=c("solid","dashed")



Psychometrics

- Classical test theory measures of reliability
 - Scoring tests
 - Reliability (alpha, beta, omega)
- Multivariate Analysis
 - Factor Analysis
 - Components analysis
 - Multidimensional scaling
 - Structural Equation Modeling
- Item Response Theory
 - One parameter (Rasch) models
 - 2PL and 2PN models



Classic theory estimates of reliabllity

- Scoring tests
 - score.items Score 1-n scales using a set of keys and finding the simple sum or average of items. Reversed items are indicated by -1
 - score.multipe.choice : Score multiple choice items by first converting to 0 or 1 and then proceeding to score the items.
- Alternative estimates of reliability
 - alpha α reliability of a single scale finds the average split half reliability. (some items may be reversed keyed).
 - omega ω_h reliability of a single scale estimates the general factor saturation of the test.
 - guttman Find the 6 Guttman reliability estimates



Using score.items to score 25 Big 5 items (taken from the bfi example

```
> keys.list <- list(Agree=c(-1,2:5),Conscientious=c(6:8,-9,-10),Extraversion=c(-11,-12,13:15),</pre>
                                Neuroticism=c(16:20), Openness = c(21,-22,23,24,-25))
> keys <- make.keys(28,keys.list,item.labels=colnames(bfi))</pre>
> score.items(keys,bfi)
Call: score.items(keys = keys, items = bfi)
(Unstandardized) Alpha:
      Agree Conscientious Extraversion Neuroticism Openness
alpha 0.7
                     0.72
                                  0.76
                                              0.81
                                                        0.6
Average item correlation:
          Agree Conscientious Extraversion Neuroticism Openness
average.r 0.32
                         0.34
                                      0.39
                                                  0.46
                                                           0.23
Guttman 6* reliability:
         Agree Conscientious Extraversion Neuroticism Openness
Lambda 6 0.7
                        0.72
                                     0.76
                                                 0.81
                                                           0.6
Scale intercorrelations corrected for attenuation
raw correlations below the diagonal, alpha on the diagonal
corrected correlations above the diagonal:
              Agree Conscientious Extraversion Neuroticism Openness
Agree
               0.70
                                          0.63
                                                    -0.245
                                                               0.23
                             0.36
Conscientious 0.26
                             0.72
                                          0.35
                                                    -0.305
                                                               0.30
Extraversion 0.46
                             0.26
                                          0.76
                                                    -0.284
                                                              0.32
Neuroticism -0.18
                           -0.23
                                         -0.22
                                                    0.812
                                                             -0.12
             0.15
                             0.19
                                         0.22
                                                    -0.086
                                                              0.60
Openness
```



score.items output, continued

Item by scale correlations:

corrected for item overlap and scale reliability

COLLECTER		rem overrap an				
	Agree	${\tt Conscientious}$	${\tt Extraversion}$	${\tt Neuroticism}$	Openness	
A1	-0.40	-0.06	-0.11	0.14	-0.14	
A2	0.67	0.23	0.40	-0.07	0.17	
A3	0.70	0.22	0.48	-0.11	0.17	
A4	0.49	0.29	0.30	-0.14	0.01	
A5	0.62	0.23	0.55	-0.23	0.18	
C1	0.13	0.53	0.19	-0.08	0.28	
C2	0.21	0.61	0.17	0.00	0.20	
C3	0.21	0.54	0.14	-0.09	0.08	
C4	-0.24	-0.66	-0.23	0.31	-0.23	
C5	-0.26	-0.59	-0.29	0.36	-0.10	
E1	-0.30	-0.06	-0.59	0.11	-0.16	
E2	-0.39	-0.25	-0.70	0.34	-0.15	
E3	0.44	0.20	0.60	-0.10	0.37	
E4	0.51	0.23	0.68	-0.22	0.04	
E5	0.34	0.40	0.55	-0.10	0.31	
N1	-0.22	-0.21	-0.11	0.76	-0.12	
N2	-0.22	-0.19	-0.12	0.74	-0.06	
N3	-0.14	-0.20	-0.14	0.74	-0.03	
N4	-0.22	-0.30	-0.39	0.62	-0.02	
N5	-0.04	-0.14	-0.19	0.55	-0.18	
01	0.16	0.20	0.31	-0.09	0.52	
02	-0.01	-0.18	-0.07	0.19	-0.45	
03	0.26	0.20	0.42	-0.07	0.61	
04	0.06	-0.02	-0.10	0.21	0.32	
05	-0.09	-0.14	-0.11	0.11	-0.53	
gender	0.25	0.11	0.12	0.14	-0.07	
${\tt education}$	0.06	0.03	0.01	-0.06	0.13	
age	0.22	0.14	0.07	-0.13	0.10	



Factor analysis of Thurstone 9 variable problem

```
> f3 <- fa(Thurstone,3) #use this built in dataset
> f3
Factor Analysis using method = minres
Call: fac(r = r, nfactors = nfactors, n.obs = n.obs, rotate = rotate,
    scores = scores, residuals = residuals, SMC = SMC, missing = FALSE,
   impute = impute, min.err = min.err, max.iter = max.iter,
    symmetric = symmetric, warnings = warnings, fm = fm, alpha = alpha)
Standardized loadings based upon correlation matrix
                      MR2 MR3 h2 u2
                MR.1
Sentences 0.91 -0.04 0.04 0.82 0.18
Vocabulary 0.89 0.06 -0.03 0.84 0.16
Sent.Completion 0.83 0.04 0.00 0.73 0.27
First.Letters 0.00 0.86 0.00 0.73 0.27
4.Letter.Words -0.01 0.74 0.10 0.63 0.37
          0.18 0.63 -0.08 0.50 0.50
Suffixes
Letter.Series 0.03 -0.01 0.84 0.72 0.28
Pedigrees 0.37 -0.05 0.47 0.50 0.50
Letter.Group -0.06 0.21 0.64 0.53 0.47
               MR1 MR2 MR3
SS loadings 2.64 1.86 1.50
Proportion Var 0.29 0.21 0.17
Cumulative Var 0.29 0.50 0.67
```

With factor correlations of MR1 MR2 MR3 MR1 1.00 0.59 0.54 MR2 0.59 1.00 0.52



MR3 0.54 0.52 1.00

Factor analysis output, continued

Measures of factor score adequacy

Test of the hypothesis that 3 factors are sufficient.

The degrees of freedom for the null model are 36 and the objective function was 5.2 with Chi Square of The degrees of freedom for the model are 12 and the objective function was 0.01

The root mean square of the residuals is 0
The df corrected root mean square of the residuals is 0.01
The number of observations was 213 with Chi Square = 2.82 with prob < 1

Tucker Lewis Index of factoring reliability = 1.027 RMSEA index = 0 and the 90 % confidence intervals are 0 0.023 BIC = -61.51 Fit based upon off diagonal values = 1

MR1 MR2 MR3
Correlation of scores with factors 0.96 0.92 0.90
Multiple R square of scores with factors 0.93 0.85 0.81
Minimum correlation of possible factor scores 0.86 0.71 0.63



Bootstrapped confidence intervals

```
> f3 <- fa(Thurstone.3.n.obs=213.n.iter=20) #to do bootstrapping</pre>
Coefficients and bootstrapped confidence intervals
                                     MR2 upper low
                                                     MR3 upper
                low
                     MR1 upper low
               0.77
                    0.91 0.96 -0.12 -0.04 0.07 -0.03
                                                     0.04 0.14
Sentences
Vocabulary
              0.85 0.89 0.95 -0.01 0.06 0.10 -0.12 -0.03 0.04
Sent.Completion 0.73 0.83 0.87 -0.04 0.04 0.13 -0.08 0.00 0.12
First.Letters
              -0.06 0.00 0.10 0.68 0.86 0.93 -0.13
                                                     0.00 0.13
4.Letter.Words -0.14 -0.01 0.07 0.58 0.74 0.86 0.01
                                                     0.10 0.25
Suffixes
            0.07 0.18 0.27 0.46 0.63 0.76 -0.20 -0.08 0.06
Letter.Series -0.04 0.03 0.13 -0.10 -0.01 0.10 0.56 0.84 0.93
         0.25 0.37 0.46 -0.16 -0.05 0.08 0.27
                                                     0.47 0.66
Pedigrees
Letter.Group
              -0.16 -0.06 0.06 0.09 0.21
                                          0.31
                                               0.44
                                                     0.64 0.79
```

Interfactor correlations and bootstrapped confidence intervals lower estimate upper

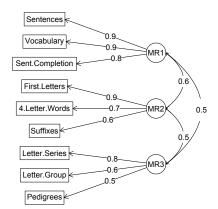
1	0.40	0.59	0.64
2	0.29	0.54	0.63
3	0.29	0.52	0.61



The simple factor structure

factor.diagram(f3) # show the diagram

Factor Analysis





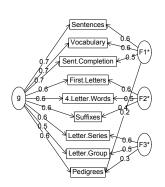
Two ways of viewing the higher order structure

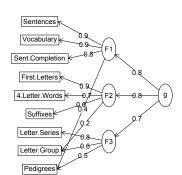
om <- omega(Thurstone)

omega.diagram(om,sl=FALSE)

Omega

Hierarchical (multilevel) Structure



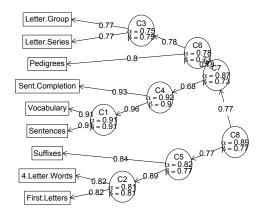




A hierarchical cluster structure found by iclust

iclust(Thurstone)

iclust





Structural Equation modeling packages

- sem (by John Fox and others)
 - uses RAM notation
- 2 lavaan (by Yves Rosseel and others)
 - Mimics as much as possible MPLUS output
 - Allows for multiple groups
 - Easy syntax
- OpenMx
 - Open source and R version of Mx
 - Allows for multiple groups (and almost anything else)
 - Complicated syntax



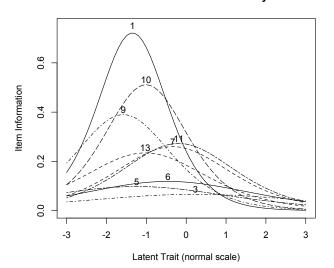
Mutiple packages to do Item Response Theory analysis

- psych uses a factor analytic procedure to estimate item discriminations and locations
 - irt.fa finds either tetrachoric or polychoric correlation matrices
 - converts factor loadings to discriminations
 - plot.irt plots item information and item characteristic functions
 - look at examples for irt.fa
 - two example data sets: igitems and bfi
- ② Other packages include Itm, eRm, mirt, + others



Item Response Information curves for 14 iq items

Item information from factor analysis





A brief technical interlude

- Data structures
 - The basic: scalers, vectors, matrices
 - More advanced data frames and lists
 - Showing the data
- Getting the length, dimensions and structure of a data structure
 - length(x), dim(x), str(x)
- Objects and Functions
 - Functions act upon objects
 - Functions actually are objects themselves
 - Getting help for a function or a package



The basic types of data structures

- Scalers (characters, integers, reals, complex)
 - > A <- 1 > B <- 2
- Vectors (of scalers, all of one type) have length

```
> C <- month.name[1:5]
> D <- 12:24
> length(D)
```

[1] 13

Matrices (all of one type) have dimensions

```
> E <- matrix(1:20, ncol = 4)
> dim(E)
```

[1] 5 4



Show values by entering the variable name

```
> A
[1] 1
> B
[1] 2
> C
[1] "January" "February" "March" "April"
                                             "May"
> D
 [1] 12 13 14 15 16 17 18 19 20 21 22 23 24
> E
     [,1] [,2] [,3] [,4]
[1,]
            6 11
                   16
[2,]
       2 7 12
                   17
[3,]
    3 8 13
                   18
[4,]
            9
                14
                    19
           10
[5,]
                15
                    20
```



More complicated (and useful) types: Data frames and Lists

• Data frames are collections of vectors and may be of different type. They have two dimensions.

```
> E.df <- data.frame(names = C, values = c(31, 28, 31, 30, 31))
> dim(E.df)

[1] 5 2
```

2 Lists are collections of what ever you want. They have length, but do not have dimensions.

```
> F <- list(first = A, a.vector = C, a.matrix = E)
> length(F)
[1] 3
```



Show values by entering the variable name

```
> E.df
    names values
              31
  January
2 February
              28
3
    March
          31
4
    April
            30
5
      May
              31
> F
$first
[1] 1
$a.vector
[1] "January" "February" "March"
                                   "April"
                                              "May"
$a.matrix
    [,1] [,2] [,3] [,4]
[1,]
            6 11
                     16
[2,]
       2 7 12
                   17
[3,] 3 8 13
                    18
       4
[4,]
                14
                    19
```

[5,]

10

15

20



Psvchometric

To show the structure of a list, use str

```
> str(F)
List of 3
 $ first : num 1
 $ a.vector: chr [1:5] "January" "February" "March" "April" ...
 $ a.matrix: int [1:5, 1:4] 1 2 3 4 5 6 7 8 9 10 ...
```

2 to address an element of a list, call it by name or number, to get a row or column of a matrix specify the row, column or both.

```
> F[[2]]
[1] "January" "February" "March"
> F[["a.matrix"]][, 2]
[1] 6 7 8 9 10
> F[["a.matrix"]][2, ]
[1] 2 7 12 17
```



"May"

"April"

Addressing the elements of a data.frame or matrix

```
Setting row and column names using paste
> E <- matrix(1:20, ncol = 4)
> colnames(E) <- paste("C", 1:ncol(E), sep = "")</pre>
> rownames(E) <- paste("R", 1:nrow(E), sep = "")
> E
   C1 C2 C3 C4
R1 1 6 11 16
R2 2 7 12 17
R3 3 8 13 18
R4 4 9 14 19
R5 5 10 15 20
> E["R2", ]
C1 C2 C3 C4
2 7 12 17
> E[, 3:4]
  C3 C4
R1 11 16
R2 12 17
R3 13 18
R4 14 19
R5 15 20
```



Objects and Functions

- R is a collection of Functions that act upon and return Objects
- ② Although most functions can act on an object and return an object (a = f(b)), some are binary operators
 - primitive arithmetic functions +, -, * , /, %*%,
 - logical functions <, > ,==, !=
- Some functions do not return values
 - print(x,digits=3)
 - summary(some object)
- But most useful functions act on an object and return a resulting object
 - this allows for extraordinary power because you can combine functions by making the output of one the input of the next.
 - The number of R functions is very large, for each package has introduced more functions, but for any one task, not many functions need to be learned.



Getting help

- All functions have a help menu
 - help(the function)

Online and hard conv books

- ? the function
- most function help pages have examples to show how to use the function
- Most packages have "vignettes" that give overviews of all the functions in the package and are somewhat more readable than the help for a specific function.
 - The examples are longer, somewhat more readable. (e.g., the vignette for psych is available either from the menu (Mac) or from http://cran.r-project.org/web/packages/psych/ vignettes/overview.pdf
- To find a function in the entire R space, use findFn in the sos package.
- Online tutorials (e.g.,http://Rpad.org for a list of important commands, http://personality-project.org/r) for a tutorial for psychologists.

A few of the most useful data manipulations functions (adapted from Rpad-refcard). Use ? for details

Psychometric

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```
dim (x) dimensions of x
file.choose () find a file
                                                       str (x) Structure of an object
file.choose (new=TRUE) create a
                                                       list (...) create a list
           new file
                                                 colnames (x) set or find column
read.table (filename)
                                                            names
  read.csv (filename) reads a
                                                rownames (x) set or find row names
           comma separated file
                                          ncol(x), nrow(z) number of row, columns
read.delim (filename) reads a tab
           delimited file
                                                     rbind (...) combine by rows
         c (...) combine arguments
                                                     cbind (...) combine by columns
   from:to e.g., 4:8
                                                     is.na (x) also is.null(x), is...
       seq (from, to, by)
                                                   na.omit (x) ignore missing data
       rep (x,times) repeat x
                                                     table (x)
        gl (n,k,...) generate factor
                                                    merge (x,y)
            levels
                                                     apply (x,rc,FUNCTION)
    matrix (x,nrow=,ncol=) create
                                                         Is () show workspace
           a matrix
                                                       rm () remove variables from
data.frame (...) create a data frame
                                                            workspace
```

More useful statistical functions, Use ? for details

```
mean (x)
                                       Selected functions from psych package
    is.na (x) also is.null(x), is...
                                               describe (x) descriptive stats
                                            describe.by (x,y) descriptives by group
 na.omit (x) ignore missing data
                                           pairs.panels (x) SPLOM
    sum (x)
                                             error.bars (x) means + error bars
rowSums (x) see also colSums(x)
     min (x)
                                          error.bars.by (x) Error bars by groups
                                                     fa (x,n) Factor analysis
    max(x)
                                              principal (x,n) Principal components
   range (x)
   table (x)
                                                 iclust (x) Item cluster analysis
                                            score.items (x) score multiple scales
summary (x) depends upon x
      sd (x) standard deviation
                                       score.multiple.choice (x) score multiple choice
                                                        scales
     cor (x) correlation
                                                 alpha (x) Cronbach's alpha
     cov (x) covariance
                                                omega (x) MacDonald's omega
   solve (x) inverse of x
                                                  irt.fa (x) Item response theory
      lm (y~x) linear model
                                                        through factor analysis
     aov (y~x) ANOVA
```

Questions?



